

1. In the Planck theory for blackbody radiation, "oscillators" occupy discrete energy levels E_0, E_1, E_2, \dots

a. What is E_0 , and what E_2 ? $E_0 = 0, E_2 = 2h\nu$

b. Which level has the largest number of oscillators: E_0, E_1 , or E_2 ?

c. Why does in contrast to the Planck theory the classical theory result in an ultra-violet catastrophe?

E_0
 E is continuous in classical theory

d. What is the ultra-violet catastrophe?

$$\lambda \rightarrow 0 \Rightarrow E \rightarrow \infty$$

2. A photoelectric experiment shows that UV light with $\lambda = 248 \text{ nm}$ is required to remove an electron from a metal plate. Given $h = 6.63 \times 10^{-34} \text{ m}^2\text{kg/s}$; $c = 2.998 \times 10^8 \text{ m/s}$, $m_e = 9.11 \times 10^{-31} \text{ kg}$,

a. What is the minimum energy required to remove an electron?

$$W = E_{\text{min}} = h\nu = h \frac{c}{\lambda} = 6.63 \times 10^{-34} \text{ m}^2\text{kg/s} \cdot \frac{2.998 \times 10^8 \text{ m/s}}{248 \text{ nm}} = 8.0 \times 10^{-19} \text{ m}^2\text{kg/s}^2$$

b. What is the electron momentum if UV light of $\lambda = 150 \text{ nm}$ is used?

$$E_{\text{tot}} = E_{\text{kin}} + W = \frac{1}{2}mv^2 + W = \frac{1}{2m}p^2 + W = h\nu = h \frac{c}{\lambda}$$

$$\Rightarrow p = \sqrt{2m(h \frac{c}{\lambda} - W)} = \sqrt{2 \times 9.11 \times 10^{-31} \text{ kg} (6.63 \times 10^{-34} \text{ m}^2\text{kg/s} \cdot \frac{2.998 \times 10^8 \text{ m/s}}{150 \times 10^{-9} \text{ m}} - 8.0 \times 10^{-19} \text{ m}^2\text{kg/s}^2)}$$

c. What is the de Broglie wavelength of the electrons in this case?

$$\lambda = \frac{h}{p} = \frac{6.63 \times 10^{-34} \text{ m}^2\text{kg/s}}{9.73 \times 10^{-25} \text{ m}^2\text{kg/s}} = 0.681 \text{ nm} \quad \left| \quad = 9.73 \times 10^{-25} \text{ m}^2\text{kg/s} \right.$$

3. Calculate, on the basis of the Bohr theory, the linear velocity of an electron in the ground state of the hydrogen atom. What is its De Broglie wavelength?

$$L = mvr = n\hbar \Rightarrow v = \frac{nh}{2\pi m r}; \quad n=1, \quad r = a_0 = 0.512 \text{ \AA}$$

$$\Rightarrow v = \frac{h}{2\pi m_e a_0} = \frac{6.63 \times 10^{-34} \text{ m}^2\text{kg/s}}{2 \times 3.14 \times 9.11 \times 10^{-31} \text{ kg} \times 0.512 \times 10^{-10} \text{ m}} = 2.26 \times 10^6 \text{ m/s}$$

$$\lambda = \frac{h}{p} = \frac{h}{mv} = \frac{6.63 \times 10^{-34} \text{ m}^2\text{kg/s}}{9.11 \times 10^{-31} \text{ kg} \times 2.26 \times 10^6 \text{ m/s}} = 3.21 \times 10^{-10} \text{ m}$$

4. Calculate the wavelength corresponding to the $n=4$ to $n=5$ transition in the hydrogen atom ($R_H = 1.0968 \times 10^7 \text{ 1/m}$).

$$\frac{1}{\lambda} = R_H \cdot \left(\frac{1}{4^2} - \frac{1}{5^2} \right) = R_H (0.0225) = 0.0247 \times 10^7 \text{ 1/m} \quad \lambda = 40.5 \times 10^{-7} \text{ m}$$