

Worksheet # 6 (Total number of points you can get is 3 pts)

1. Assume **adiabatic** reversible compression of 1 mol of an ideal gas from (P_1, V_1, T_1) to (P_2, V_2, T_2) . (Draw P-V diagram!)

a. Does the temperature T increase or decrease? Why?

$$\frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma-1}; \quad V_1 > V_2 \text{ and } \gamma > 1 \Rightarrow T_2 > T_1$$

b. Write down the reversible work in terms of heat capacity and temperature.

$$W_{rev} = \Delta U - Q = \Delta U = C_V (T_2 - T_1)$$

c. Compare with reversible **isothermal** compression from the same starting conditions (P_1, V_1, T_1) to a new state (P_2^*, V_2, T_1) . Is P_2^* larger or smaller than P_2 ? Why?

$$\left. \begin{array}{l} \text{isothermal: } P_1 V_1 = P_2^* V_2 \\ \text{adiabatic: } P_1 V_1^\gamma = P_2 V_2^\gamma \end{array} \right\} P_2^* = P_2 \left(\frac{V_2}{V_1}\right)^{\gamma-1}$$

$$\gamma > 1, V_2 < V_1 \Rightarrow P_2^* < P_2$$

2. One mol of an ideal gas is reversibly expanded at constant temperature until $V_2 = 3 V_1$. If the gas performed 3 kJ of work, what is its temperature?

$$W = RT \ln \frac{V_1}{V_2} \Rightarrow T = \frac{W}{R \ln \frac{V_1}{V_2}}$$

$$= \frac{-3 \cdot 10^3 \text{ J}}{-8.3145 \frac{\text{J}}{\text{K}} \cdot \ln 3}$$

$$= \frac{3 \cdot 10^3}{8.3145 \cdot 1.099} = 328.4 \text{ K}$$

3. Why is the energetics of chemical reactions often described by enthalpy differences ΔH , instead of internal energy differences ΔU ?

Experimental condition is usually $P = \text{const}$