

## Worksheet #11 (Total number of points you can get is 3 pts)

1. Assume an ideal solution of two components A and B. At T=300 K,  $P^*(A) = 3$  kPa, and  $P^*(B) = 9$  kPa. Compute the vapor pressure of a solution containing 0.6 mol fraction of A. What is the mole fraction of A in the vapor over

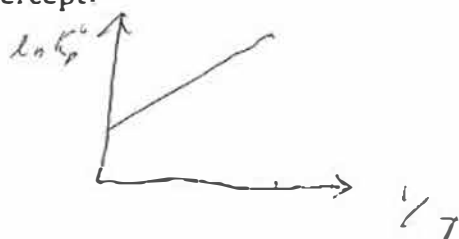
the liquid?

$$P = \chi_A P_A^* + (1 - \chi_A) P_B^* = 0.6 \cdot 3 \times 10^3 \text{ Pa} + 0.4 \cdot 9 \times 10^3 \text{ Pa}$$

$$= 5.4 \times 10^3 \text{ Pa} = 5.4 \text{ kPa}$$

$$P_A = \chi_A^{\text{vap}} P \Rightarrow \chi_A^{\text{vap}} = \frac{P_A}{P} = \frac{\chi_A P_A^*}{P} = \frac{1.8 \text{ kPa}}{5.4 \text{ kPa}} = 0.33$$

2. Assume that in a chemical reaction  $\Delta H^\circ$  does not depend on temperature.
- a. Draw a van't Hoff plot, i.e.  $\ln K_p^\circ$  over  $1/T$ . What thermodynamic quantity can be obtained from the slope, and what quantity from the intercept?



$$\text{Slope: } -\frac{\Delta H^\circ}{R}$$

$$\text{Intercept: } \frac{\Delta S^\circ}{R}$$

- b. If the temperature is increased from  $T_1 = 30^\circ\text{C}$  to  $T_2 = 70^\circ\text{C}$ , what is the ratio between the equilibrium constants  $K_1^\circ$  and  $K_2^\circ$ ? ( $\Delta H^\circ = 150$ ).

$$\ln K_1^\circ = -\frac{\Delta H^\circ}{RT_1} + \frac{\Delta S^\circ}{R}; \quad \ln K_2^\circ = -\frac{\Delta H^\circ}{RT_2} + \frac{\Delta S^\circ}{R}$$

$$\Rightarrow \ln K_2^\circ - \ln K_1^\circ = \ln \frac{K_2^\circ}{K_1^\circ} = -\frac{\Delta H^\circ}{R} \left( \frac{1}{T_2} - \frac{1}{T_1} \right) = \frac{\Delta H^\circ}{R} \left( \frac{1}{T_1} - \frac{1}{T_2} \right)$$

$$\Rightarrow \frac{K_2^\circ}{K_1^\circ} = \exp \left( \frac{\Delta H^\circ}{R} \left( \frac{1}{T_1} - \frac{1}{T_2} \right) \right) = \exp \left( \frac{150 \cdot 40}{8.3145 \cdot 303.15 \cdot 343.15} \right) = e^{0.0067} = 1.007$$

3. In an experiment, the vapor pressure of a liquid is measured as 5 kPa at 300K, and as 120 kPa at 400 K. Calculate from these data the enthalpy of vaporization  $\Delta_{\text{vap}}H$  of the liquid.

$$\ln \frac{P_2}{P_1} = \frac{\Delta_{\text{vap}}H}{R} \left( \frac{1}{T_1} - \frac{1}{T_2} \right) = \frac{\Delta_{\text{vap}}H}{R} \frac{T_2 - T_1}{T_1 T_2}$$

$$\Rightarrow \Delta_{\text{vap}}H = R \ln \frac{P_2}{P_1} \frac{T_1 T_2}{T_2 - T_1} = 8.3145 \cdot \ln \frac{120}{5} \cdot \frac{300 \cdot 400}{100} \text{ J/mol}$$

$$= 8.3145 \cdot 3.1781 \cdot 1200 \text{ J/mol}$$

$$= 31.71 \text{ kJ/mol}$$